



Cálculos cuánticos ab initio en ciencia de materiales



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- Juan Ríos – CINVESTAV
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- Pablo Palacios –
- Gregorio García –
- José C. Conesa – CSIC
- Diego Solís – UNAM
- Juan L. Peña - CINVESTAV

Outline

- Solar cells
- Quantum mechanics calculations
- Defects in CdTe
- Halide perovskites

Tipos de celdas fotovoltaicas

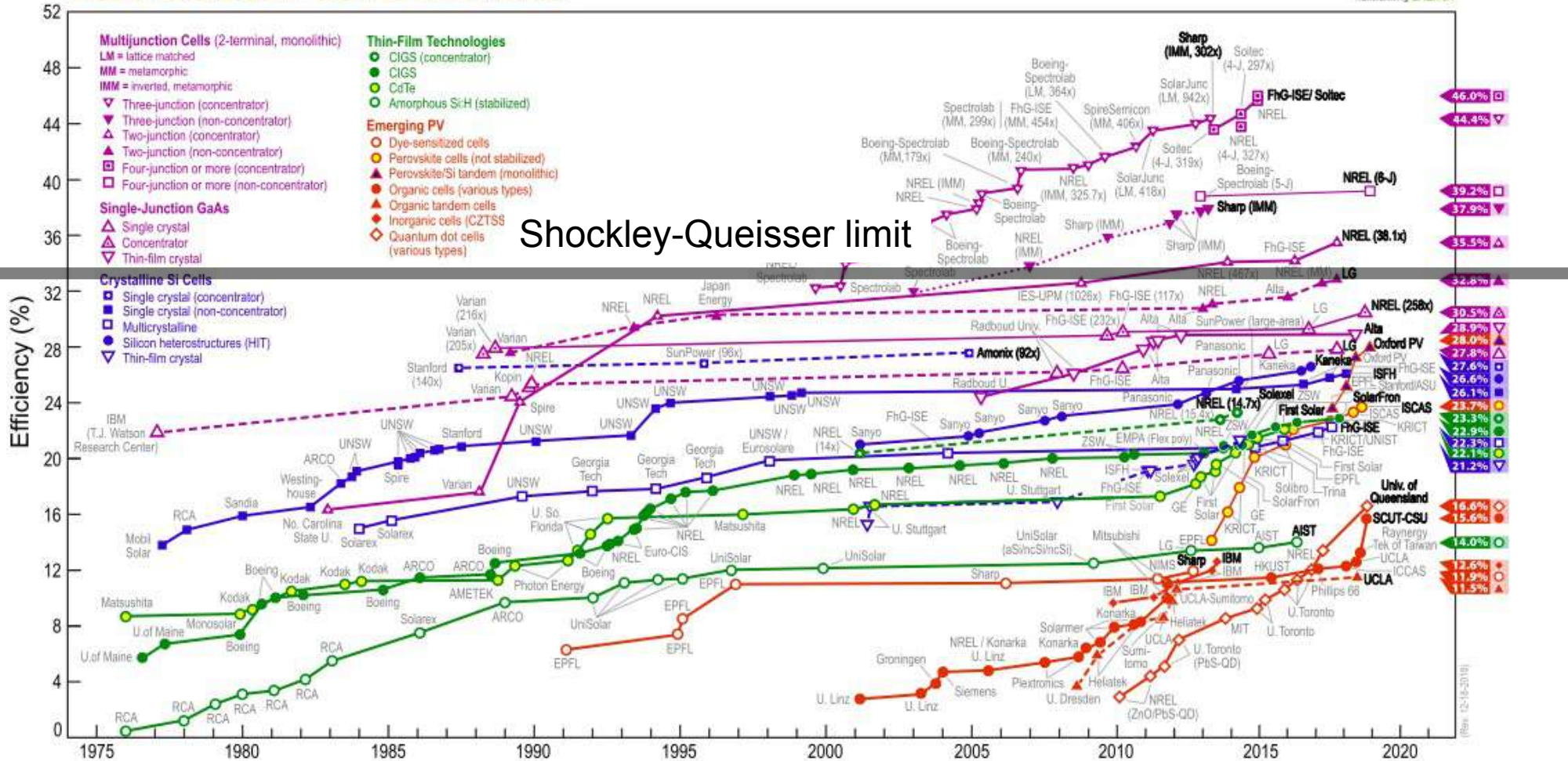
- **Silicio cristalino** (comercial, optimizada)
- **Capa delgada** (comercial, en desarrollo)
- Celdas de colorante (laboratorio)
- Orgánicas (laboratorio)
- Tandem (laboratorio)



Evolución tecnológica

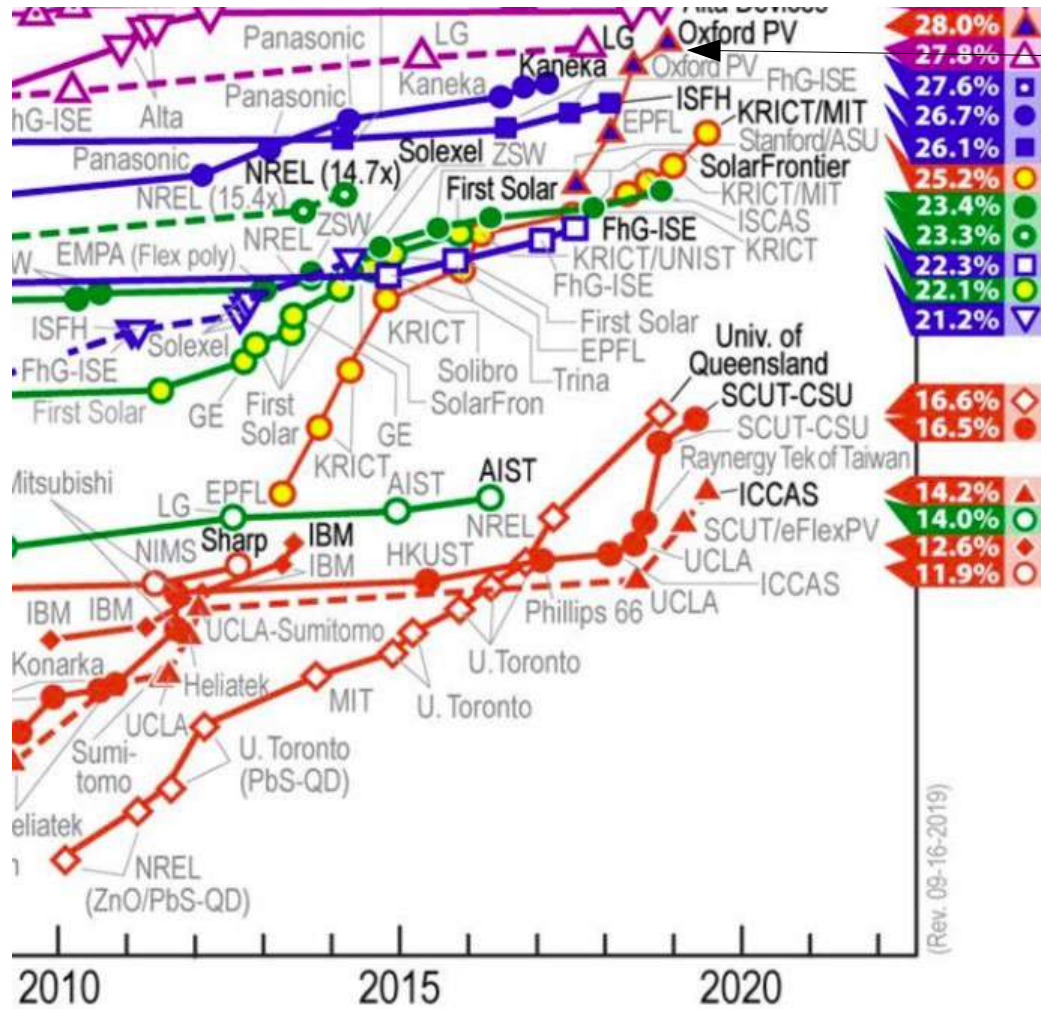
$$\text{Eficiencia} = \frac{\text{Energía eléctrica producida}}{\text{Energía solar recibida}}$$

Best Research-Cell Efficiencies



Low cost PV technologies with record efficiency > 20%

NREL chart of record efficiencies

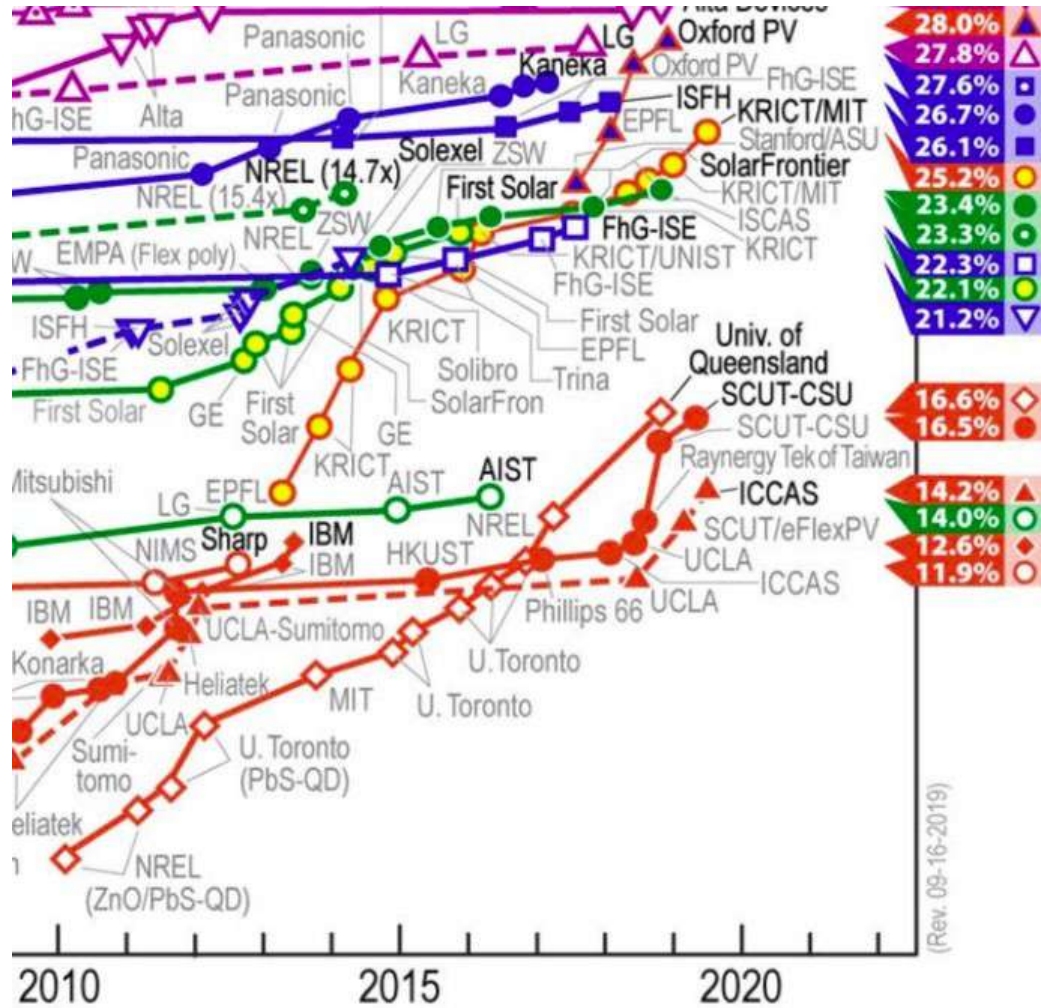


m-Si, Si/PSC
PSC(perovskite)
CIGS
CdTe/CdS

(Rev. 09-16-2019)

Área de nuestro trabajo

NREL chart of record efficiencies

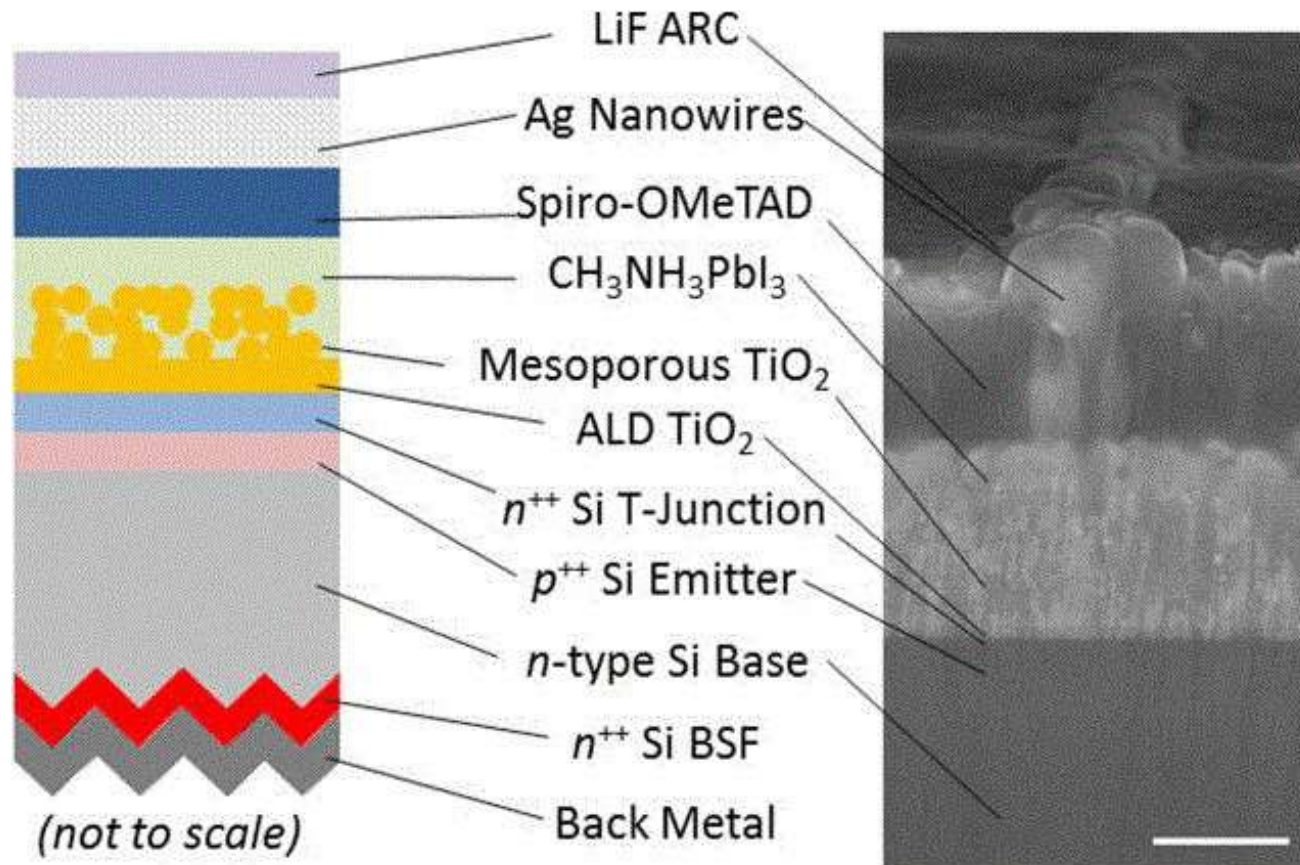


PSC(perovskite)

CdTe/CdS

(Rev. 09-16-2019)

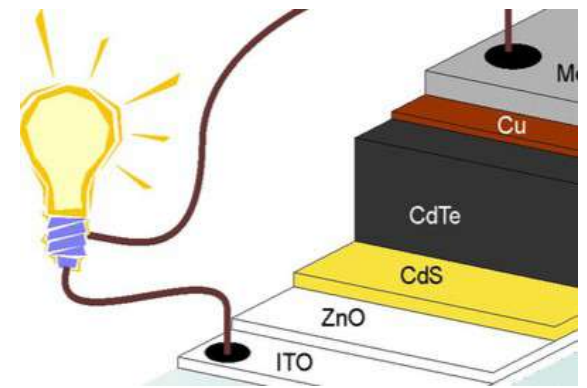
The Next Generation solar cells tandem Si/perovskite



Source: Applied Physics Letters

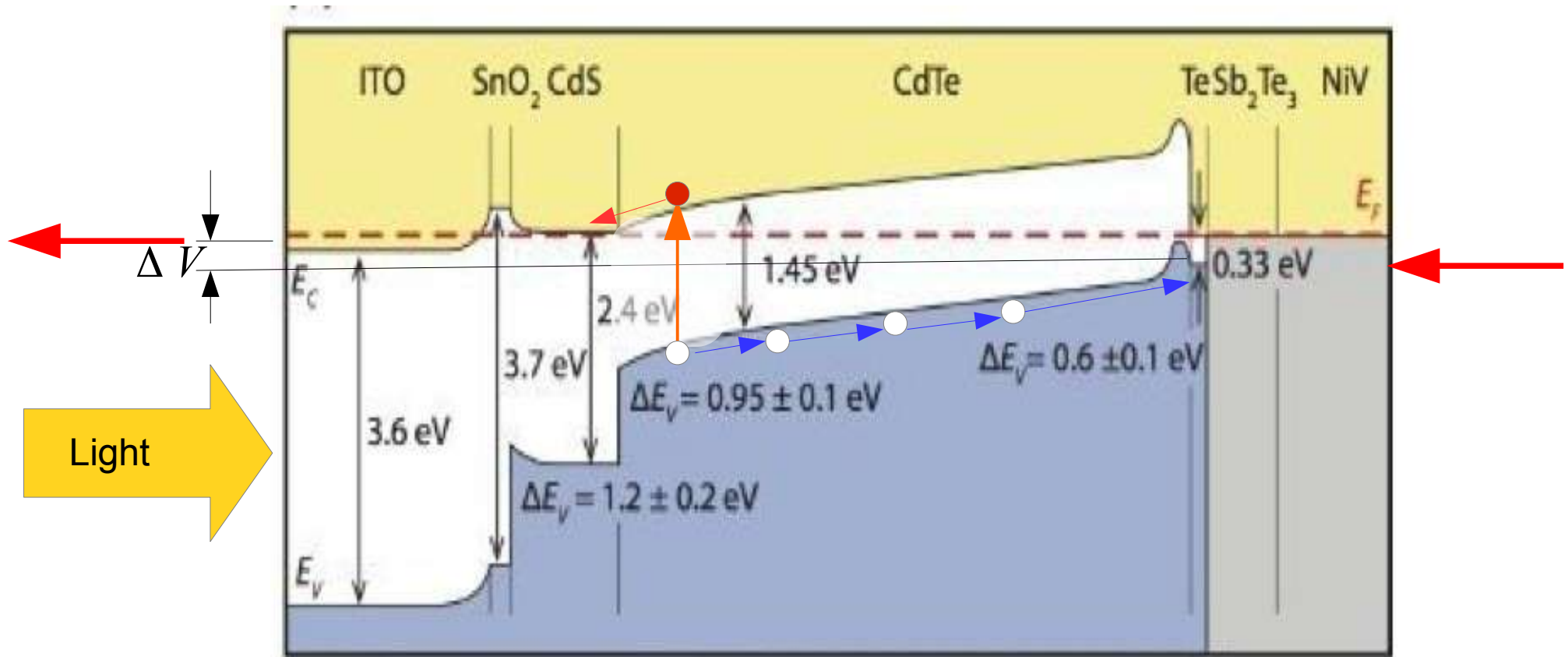
Oxford PV is building a factory

Example: CdTe/CdS solar cell ($\eta > 22\%$)



The Fermi level determines how do the bands align across de interfaces.

High hole conductivity is needed for the holes to reach the back contact.



Source: A. Smetz et al, Solar Energy, UIT Cambridge (2018).

Our approach: quantum calculations at the atomic scale

Method

Density Functional Theory (DFT)

Hohenberg, Pierre; Walter Kohn (1964).

"Inhomogeneous electron gas". Phys. Rev. 136 (3B): B864–B871.

Software



Hardware and support from NLHPC



<http://www.nlhpc.cl>

Details:

Basis sets: plane waves

Pseudopotentials

Structural optimization with van der Waals corrections.

Wavefunctions and energies from hybrid functionals

DFT Kohn-Sham equation (1965)

The ground state energy is given by

$$E_{total} = \sum_{i=1}^N f_i \langle \phi_i | -\frac{1}{2} \nabla^2 + V(\mathbf{r}) | \phi_i \rangle + \frac{1}{2} \iint d\mathbf{r} d\mathbf{r}' \frac{n(\mathbf{r})n(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} + E_{xc}[n(\mathbf{r})]$$

Initial guess for density: $n(\mathbf{r})$

$$V_{eff}(\mathbf{r}) = V(\mathbf{r}) + \int d\mathbf{r}' \frac{n(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} + v_{xc}(\mathbf{r}), \quad \text{con } v_{xc}(\mathbf{r}) = \frac{\delta E_{xc}}{\delta n(\mathbf{r})}$$

$$\left(-\frac{1}{2} \nabla^2 + V_{eff}(\mathbf{r}) \right) \phi_i(\mathbf{r}) = \epsilon_i \phi_i(\mathbf{r}) \rightarrow \{ \epsilon_i, \phi_i(\mathbf{r}) \} \rightarrow$$

$$\rightarrow n_{nueva}(\mathbf{r}) = \sum_i f_i |\phi_i(\mathbf{r})|^2, \quad 0 \leq f_i \leq 1 \text{ is the occupation number}$$

compare $n_{new}(\mathbf{r})$ con $n(\mathbf{r})$

if not equal, then $n(\mathbf{r}) = \alpha n_{nueva}(\mathbf{r}) + (1-\alpha)n(\mathbf{r})$

DFT Kohn-Sham equation (1965)

The ground state energy is given by

$E_{total} =$

Initial $V_{eff}(\mathbf{r}) =$

$\left(-\frac{1}{2} \nabla^2 + V_{eff}(\mathbf{r}) \right) \psi = E_{total} \psi$

$\rightarrow n_{nuc}$

comp if not

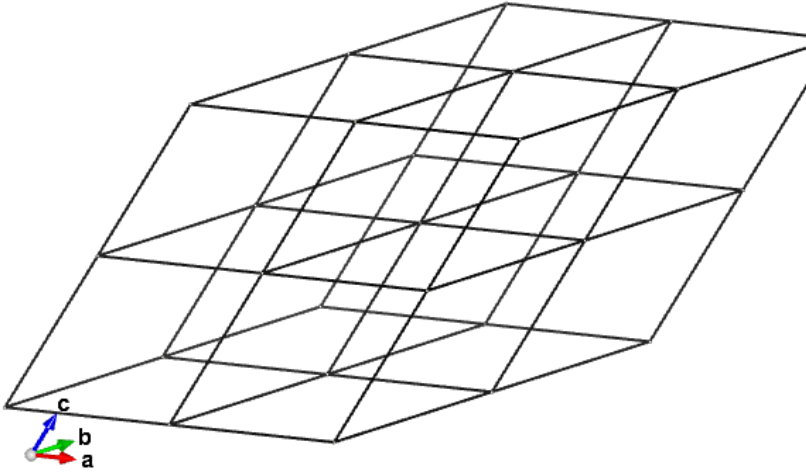
```
implicit none
real(DP) :: rho, ec, vc, ex, vx
real(DP) :: ec__, vc__
!
real(DP), parameter :: small = 1.E-10_DP, third = 1.0_DP / 3.0_DP, &
    pi34 = 0.6203504908994_DP ! pi34=(3/4pi)^(1/3)
real(DP) :: rs
!
if (rho <= small) then
    ec = 0.0_DP
    vc = 0.0_DP
    ex = 0.0_DP
    vx = 0.0_DP
    return
else
    rs = pi34 / rho**third
    ! rs as in the theory of metals: rs=(3/(4pi rho))^(1/3)
endif
!..exchange
if (iexch == 1) THEN ! 'sla'
    call slater (rs, ex, vx)
ELSEIF (iexch == 2) THEN ! 'sl1'
    call slater1(rs, ex, vx)
ELSEIF (iexch == 3) THEN ! 'rxc'
```

$E_{xc}[n(\mathbf{r})]$

er

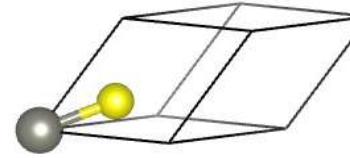
Estructura cristalina periódica

Red de Bravais



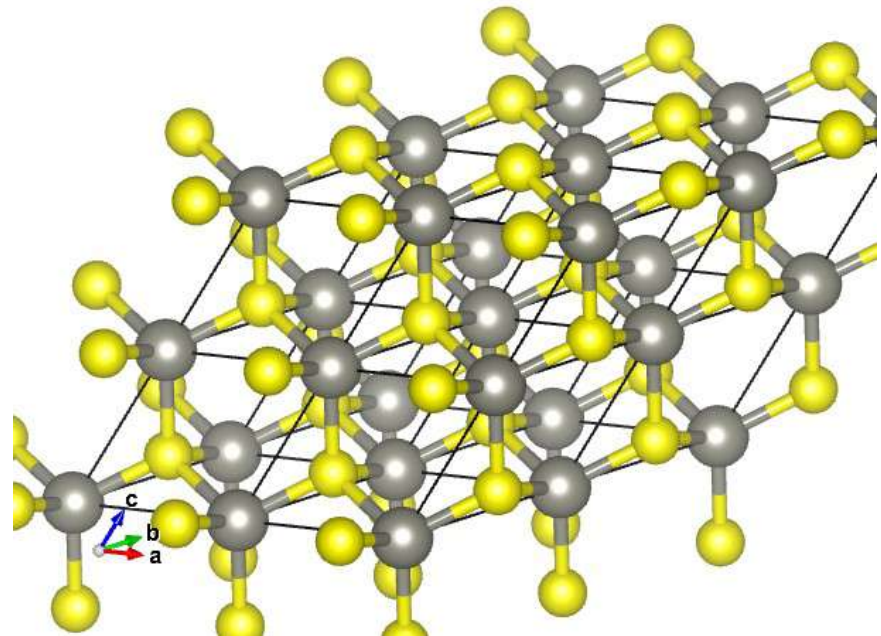
$$\vec{R}_{n_1 n_2 n_3} = n_1 \vec{a}_1 + n_2 \vec{a}_2 + n_3 \vec{a}_3$$
$$n_i = 0, \pm 1, \pm 2, \pm 3, \dots$$

+ Base



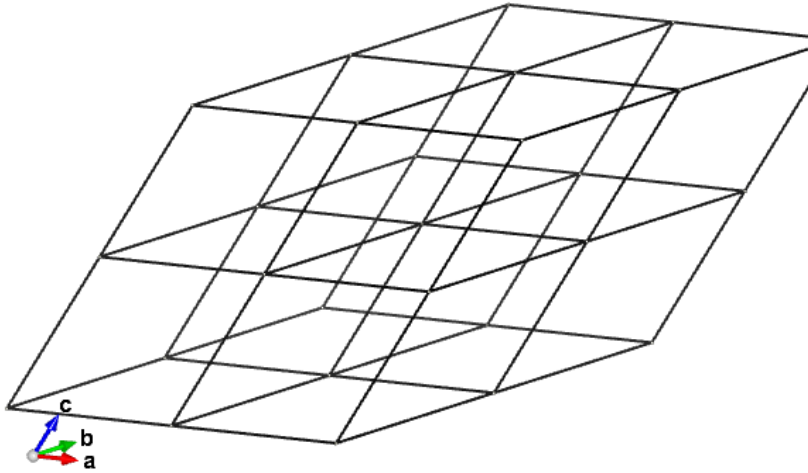
$\vec{\tau}_a$ posición del átomo a
respecto al punto de la red

Cristal: $\vec{R}_{n_1 n_2 n_3 a} = \vec{R}_{n_1 n_2 n_3} + \vec{\tau}_a$



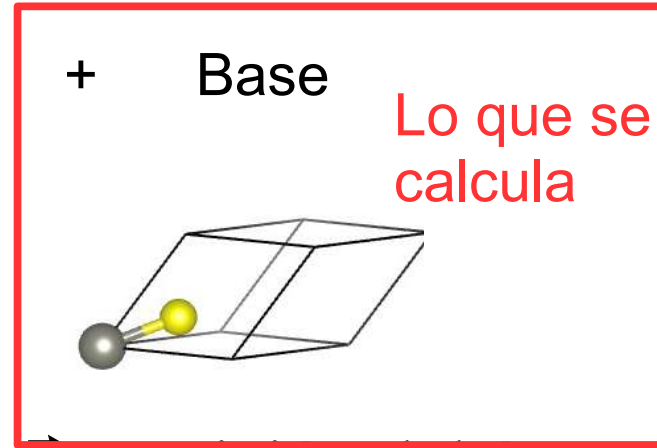
Estructura cristalina periódica

Red de Bravais

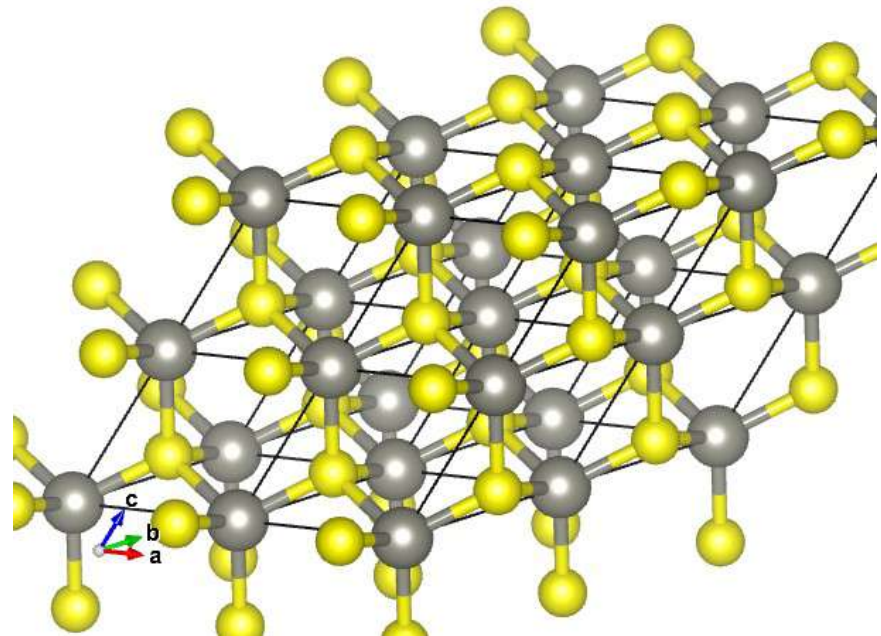


$$\vec{R}_{n_1 n_2 n_3} = n_1 \vec{a}_1 + n_2 \vec{a}_2 + n_3 \vec{a}_3$$
$$n_i = 0, \pm 1, \pm 2, \pm 3, \dots$$

Cristal: $\vec{R}_{n_1 n_2 n_3 a} = R_{n_1 n_2 n_3}^{\rightarrow} + \vec{\tau}_a$



$\vec{\tau}_a$ posición del átomo a
respecto al punto de la red



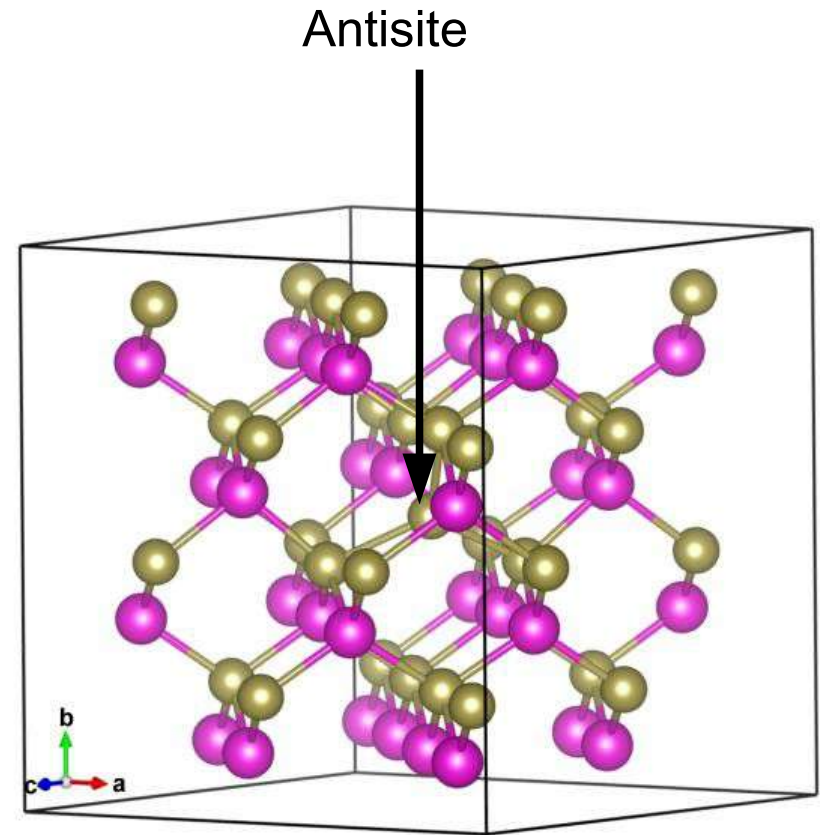
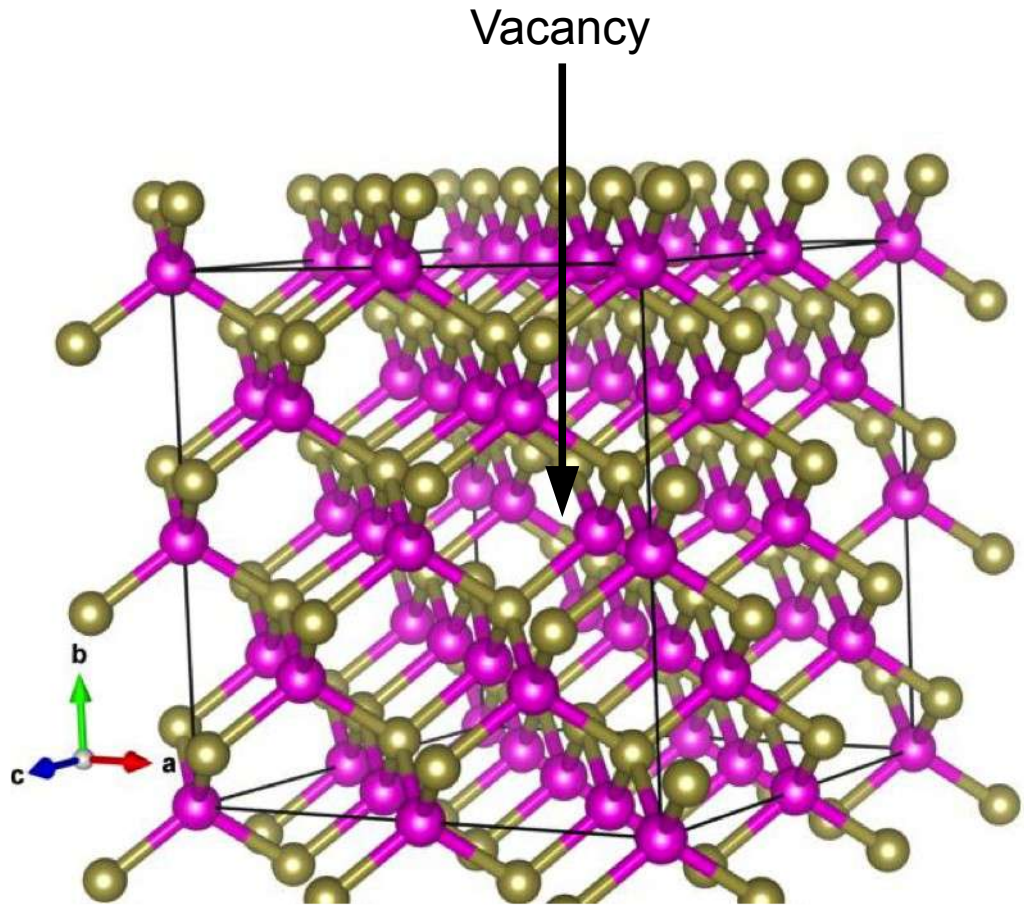
Situaciones en que la periodicidad es rota y necesitamos la escala de dimensiones relevante requiere simular muchos átomos.

Defectos

Interfaces

Nanoestructuras

Intrinsic defects



Other defects: self-interstitials, di-vacancies, vacancy-interstitial, etc

Always present:

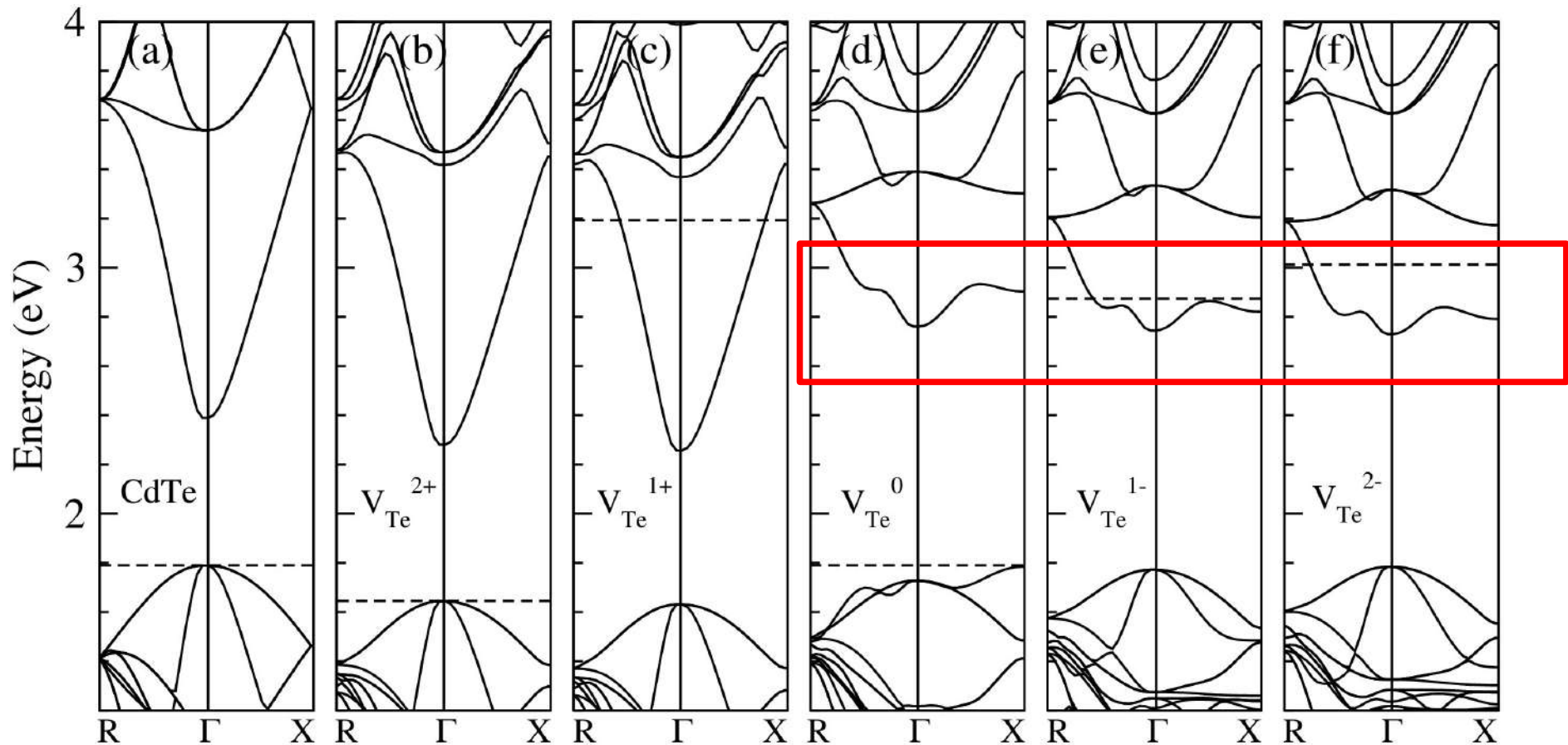
Thermodynamic concentration:
$$N_i = N_{sites} N_{config} \exp\left(\frac{-\Delta H^f}{k_B T}\right)$$

Formation energy

Materials are like people: it's the defects that make them interesting

Bands for *standard* supercells $\text{Cd}_{32}\text{Te}_{32}/\text{Cd}_{32}\text{Te}_{31}$

Phys. Status Solidi B 252, 2649-2656 (2015)

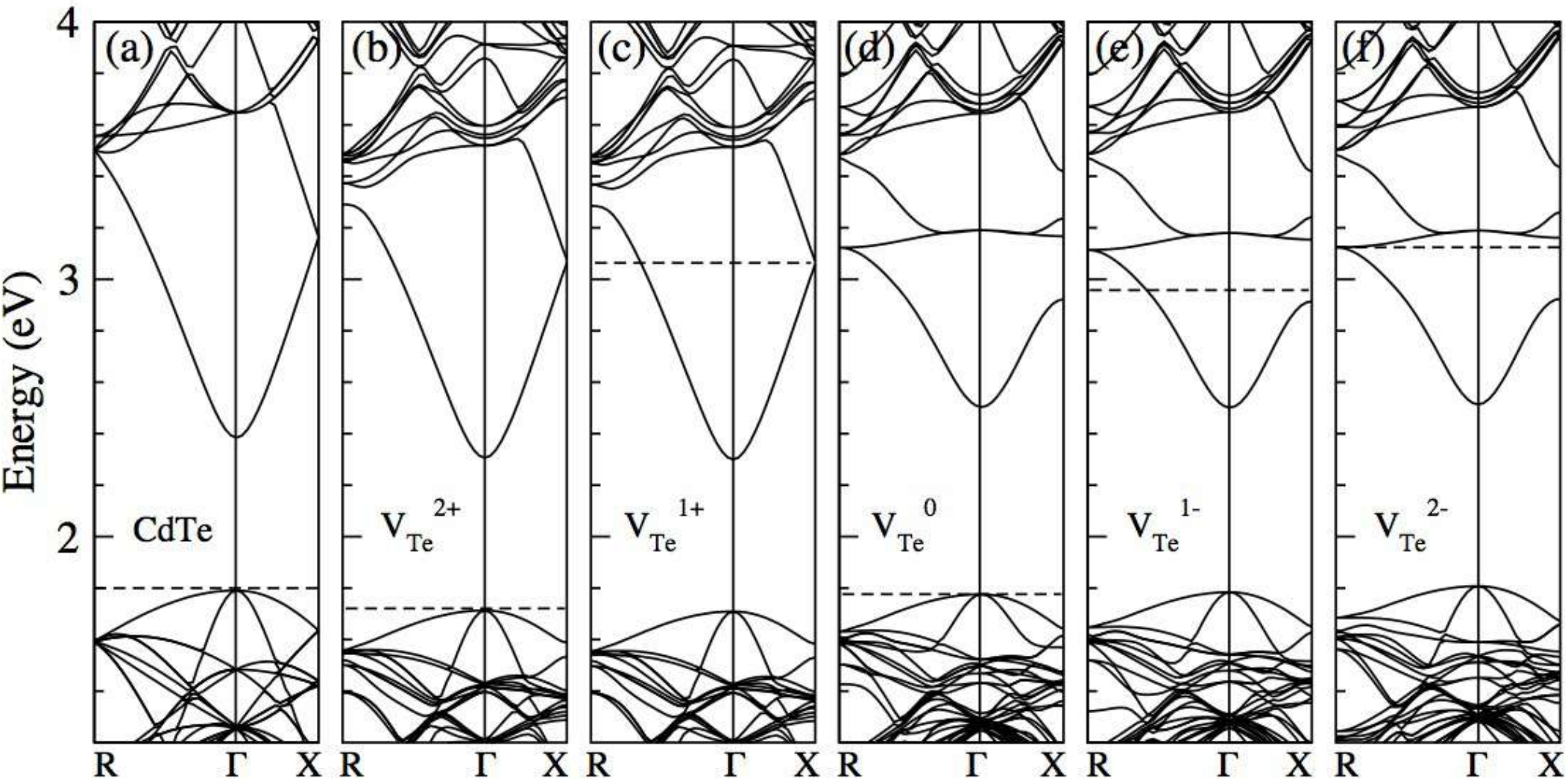


A diluted point defect is not expected to destroy the conduction band. A point defect is a perturbation.

The standard 64/63 atom supercell is not appropriate.

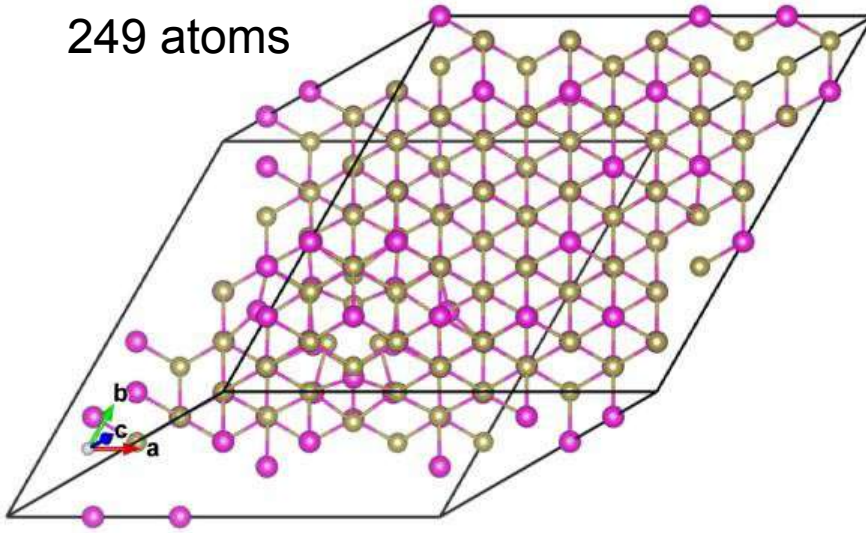
I acknowledge advice by P. Wahnón to plot the bands, even when defects are not periodic systems by definitions.

Bands for $\text{Cd}_{128}\text{Te}_{128}/\text{Cd}_{128}\text{Te}_{127}$ supercells

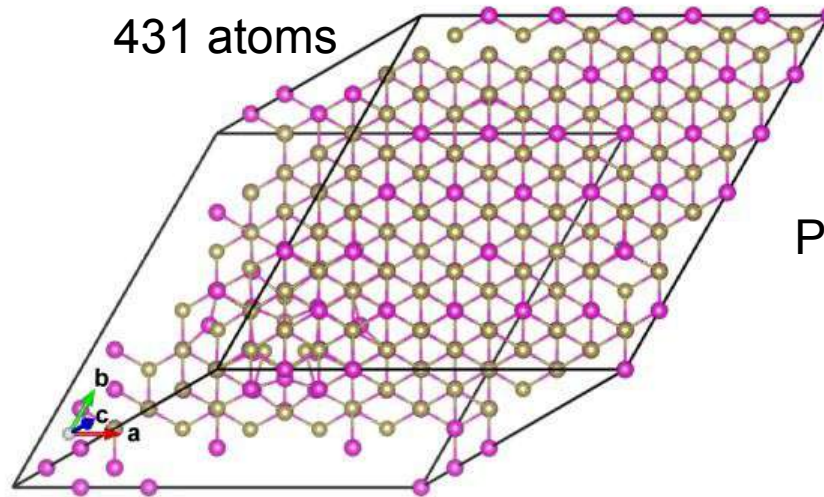


A test for V_{Cd} $q=+2$, and 0

249 atoms

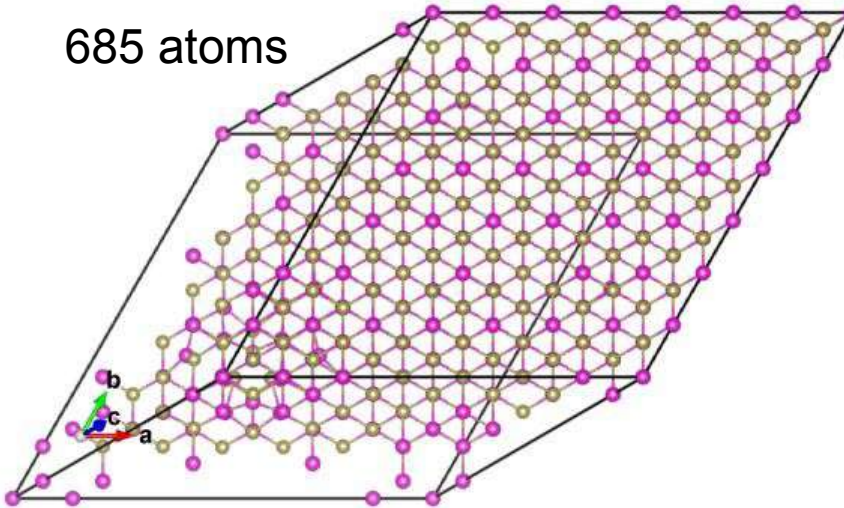


431 atoms

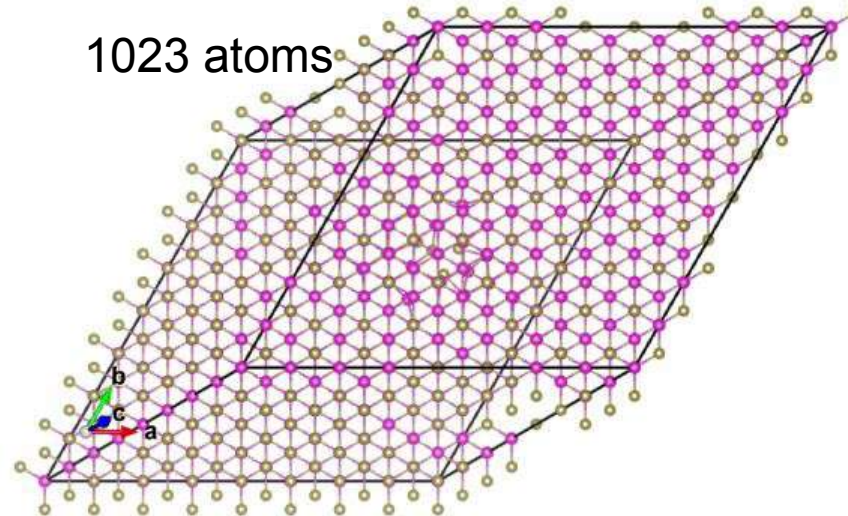


PBE functional

685 atoms

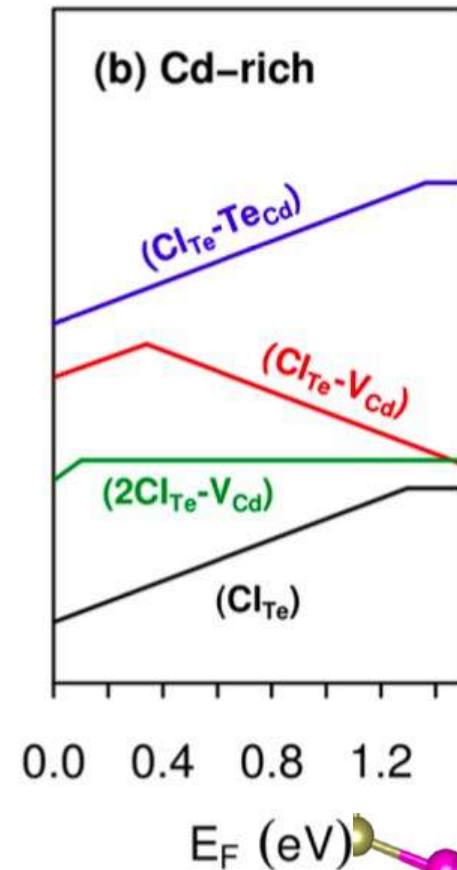
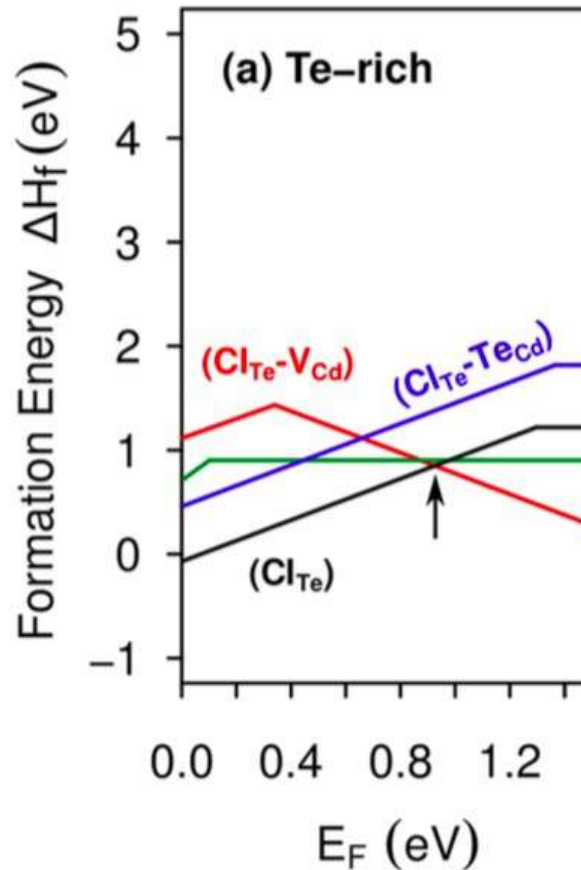
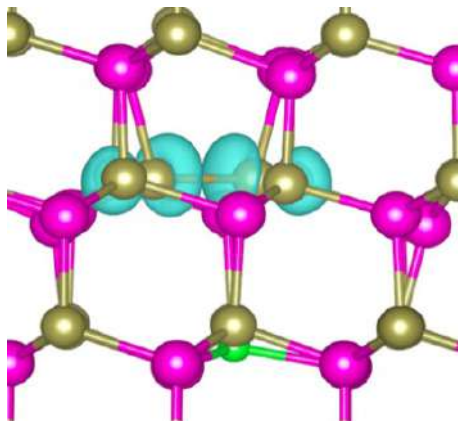


1023 atoms



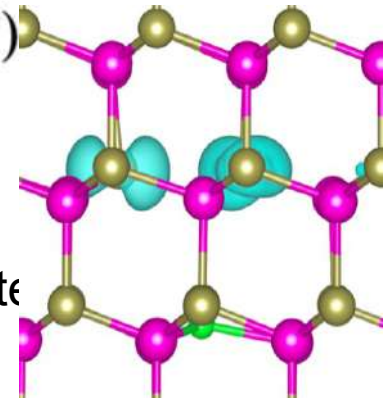
Cl-defects: Formation energy

Cl-doping is an important step in the manufacturing process of CdTe/CdS solar cells.



Lowest energy: $(Cl_{Te})^+$, $(Cl_{Te}-V_{Cd})^-$, $(2Cl_{Te}-V_{Cd})^0$

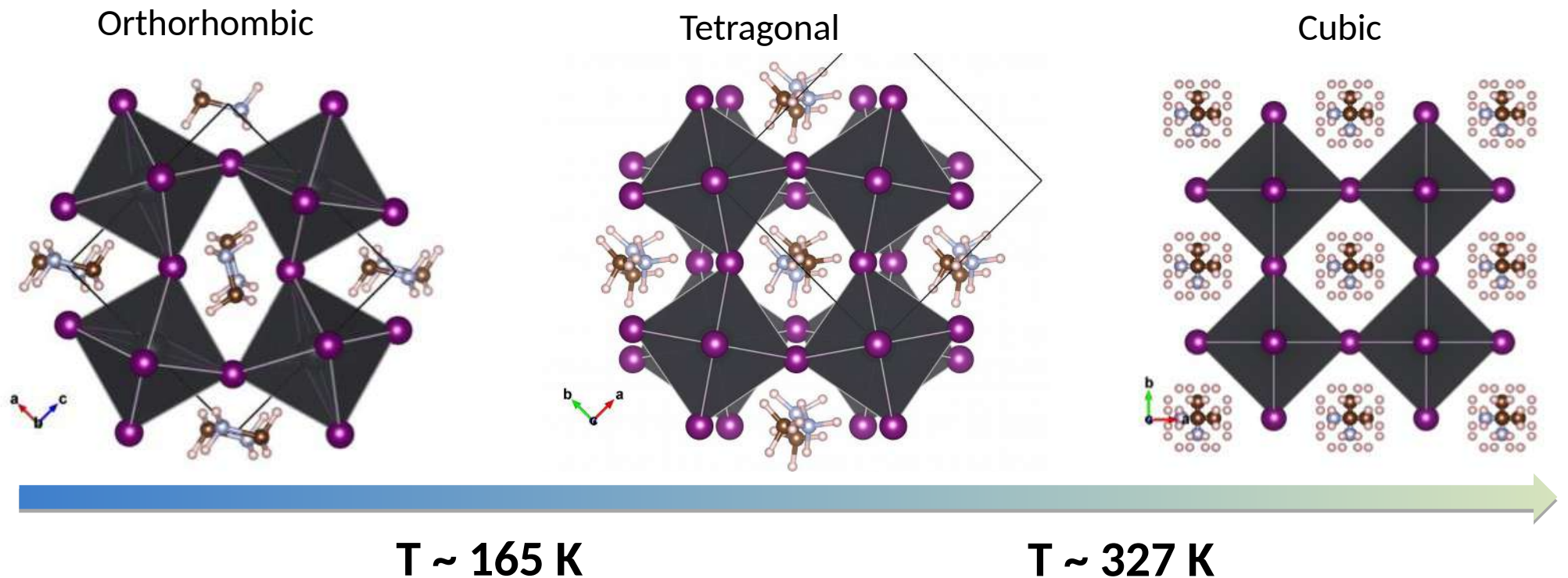
If Cl concentration is higher than that of native defect, the arrow indicates the Fermi level position.



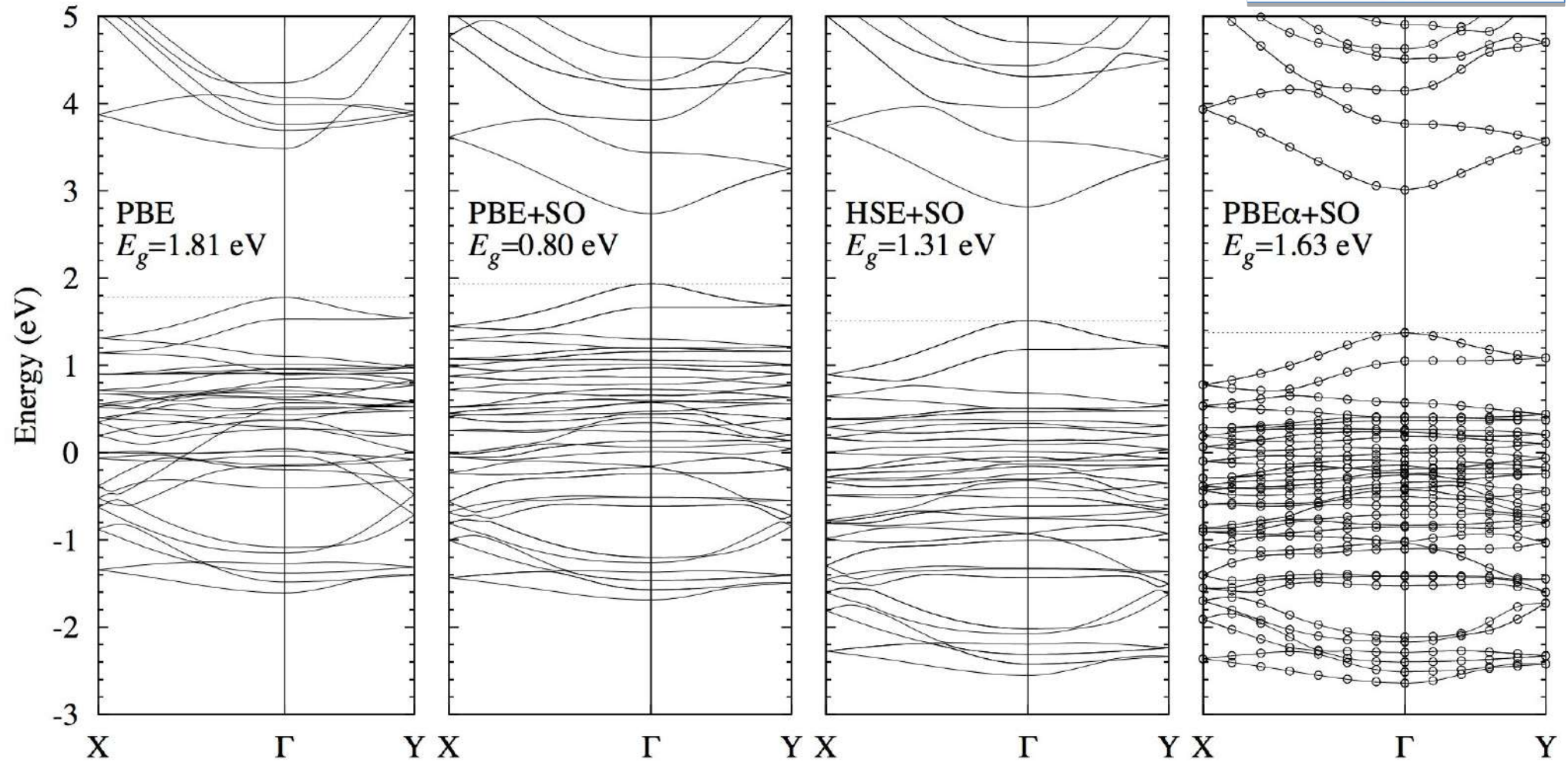
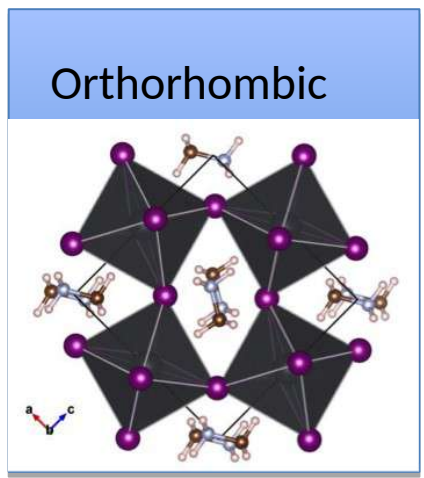
WHY STUDY THE PEROVSKITE?

MAPI Perovskite

Methylammonium-Lead-Iodide



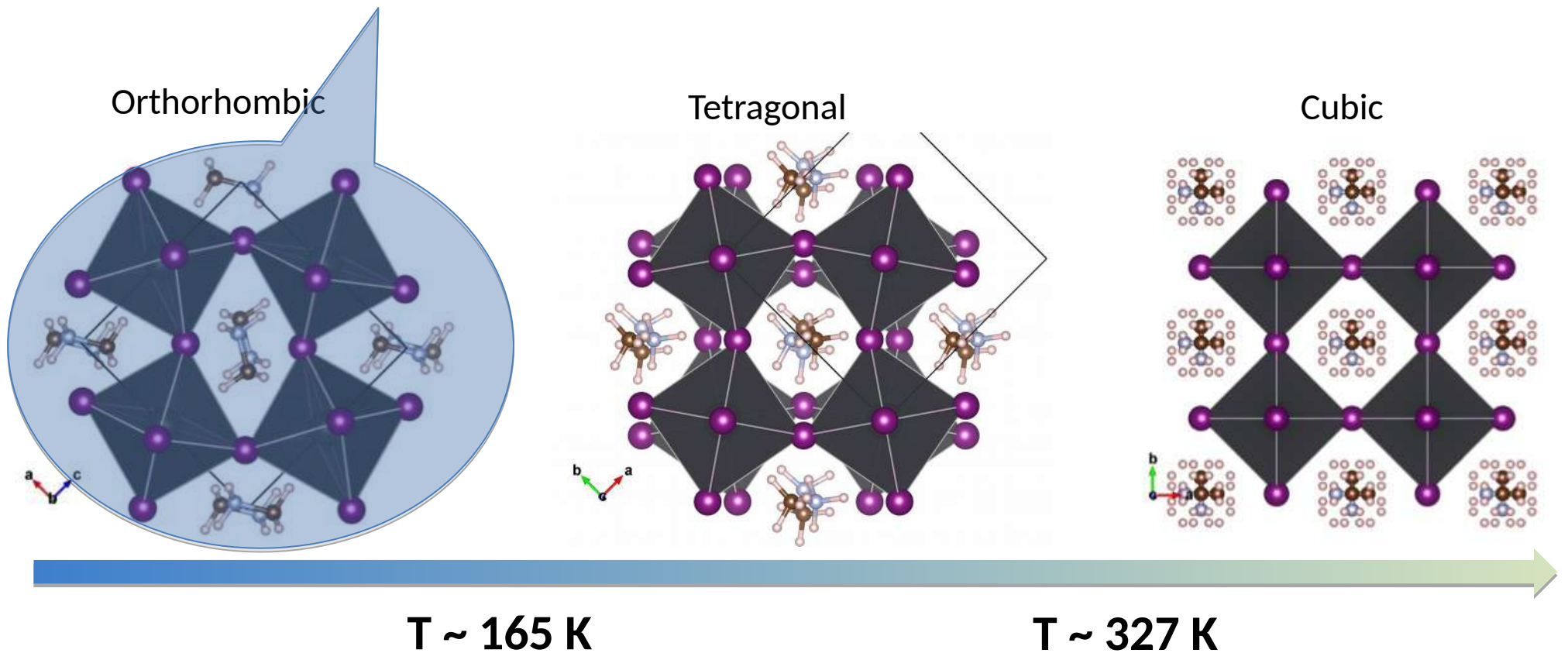
Band Diagrams with different DFT approximations



STUDY of $\text{CH}_3\text{NH}_3\text{PbI}_3$

How can we ensure that one of the high temperature phases is being simulated properly?

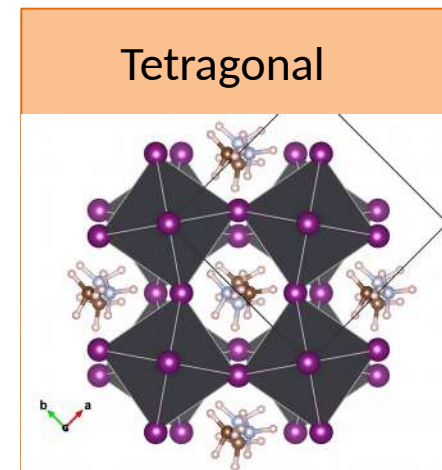
Good OK model !!!



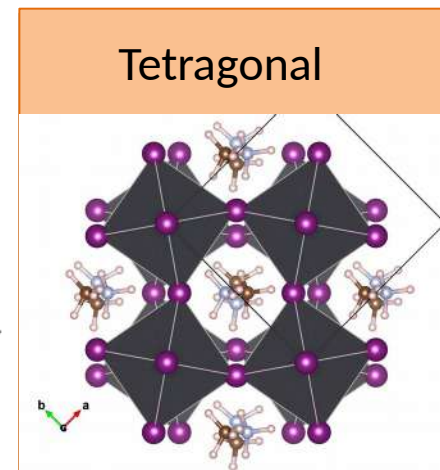
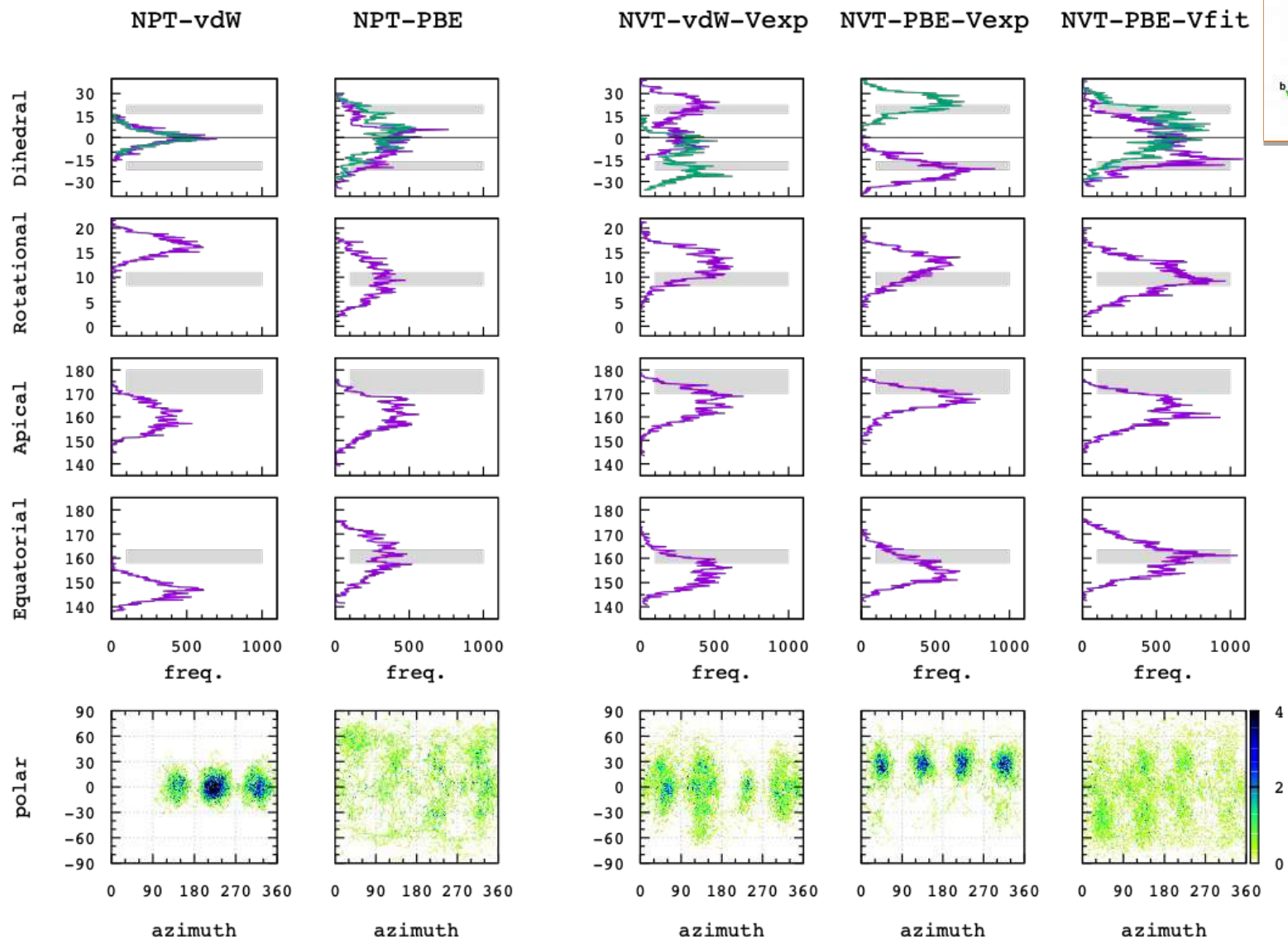
Thermal effect

Ab initio Molecular Dynamic

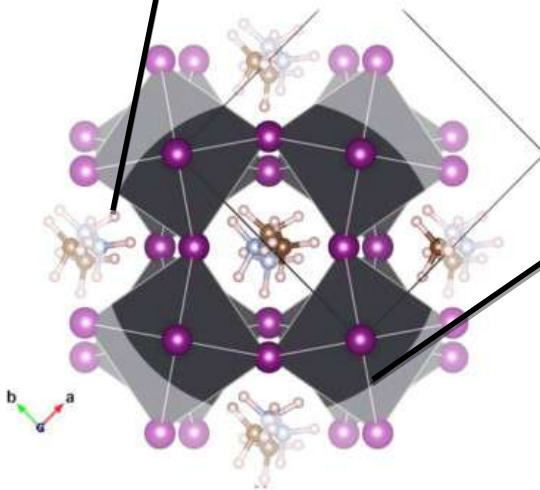
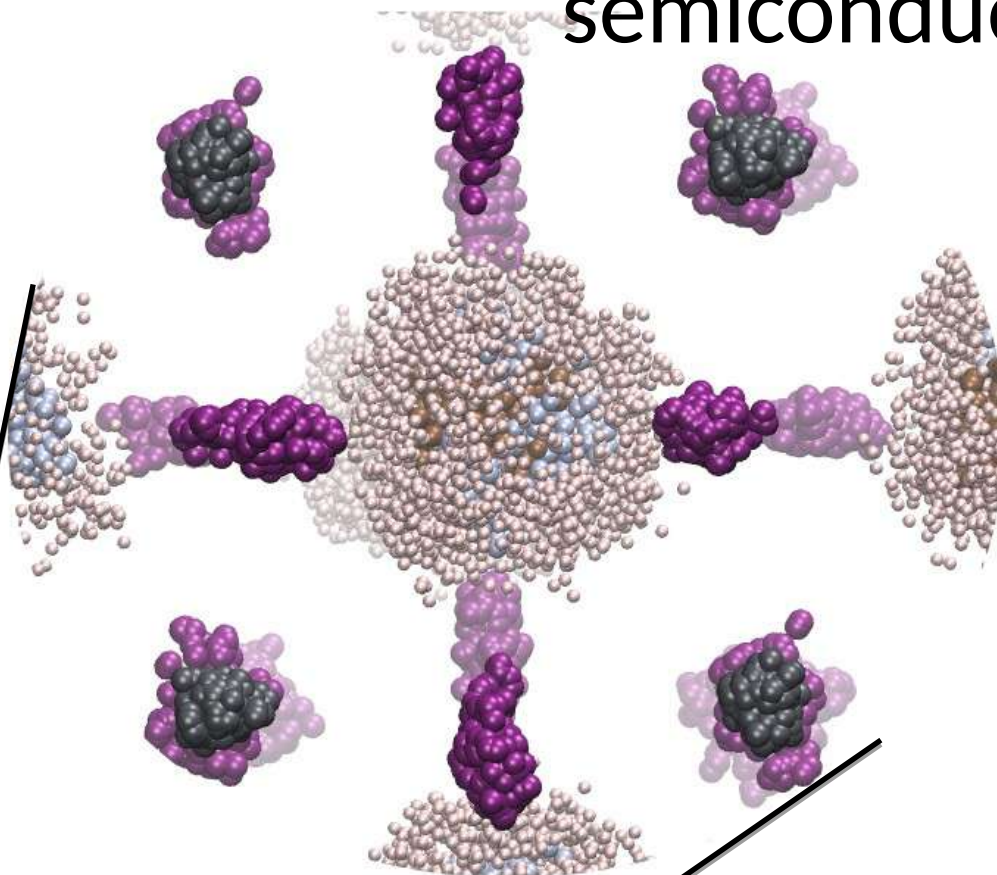
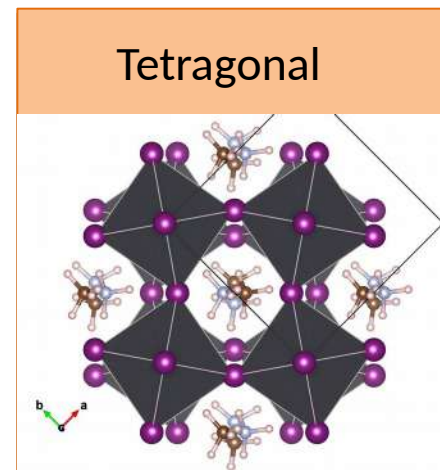
- NPT and NVT ensembles
- PBE and vdW functionals
- Relatively long simulation time (up to 100 ps)
- $T = 220$ K (Langevin thermostat)
- 1 fs of time step



Thermal effect

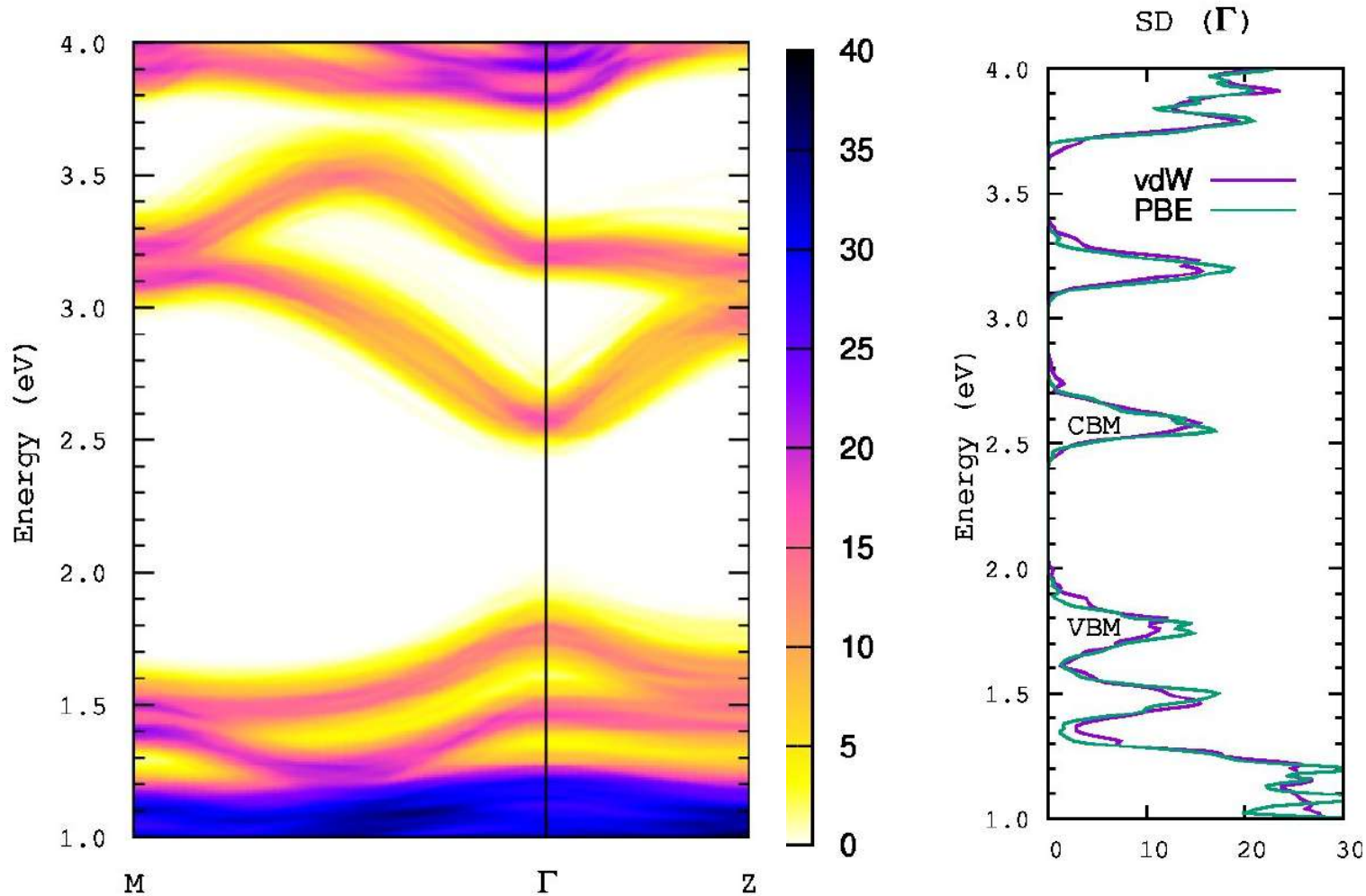
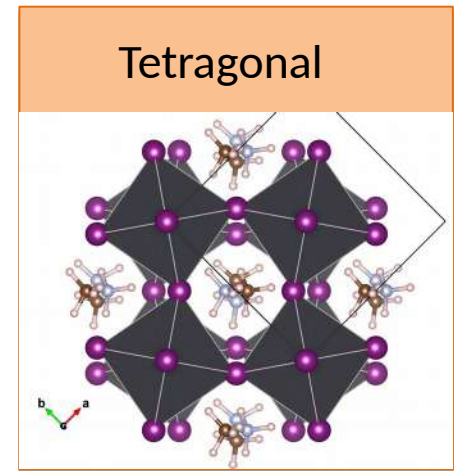


Flexible semiconductor

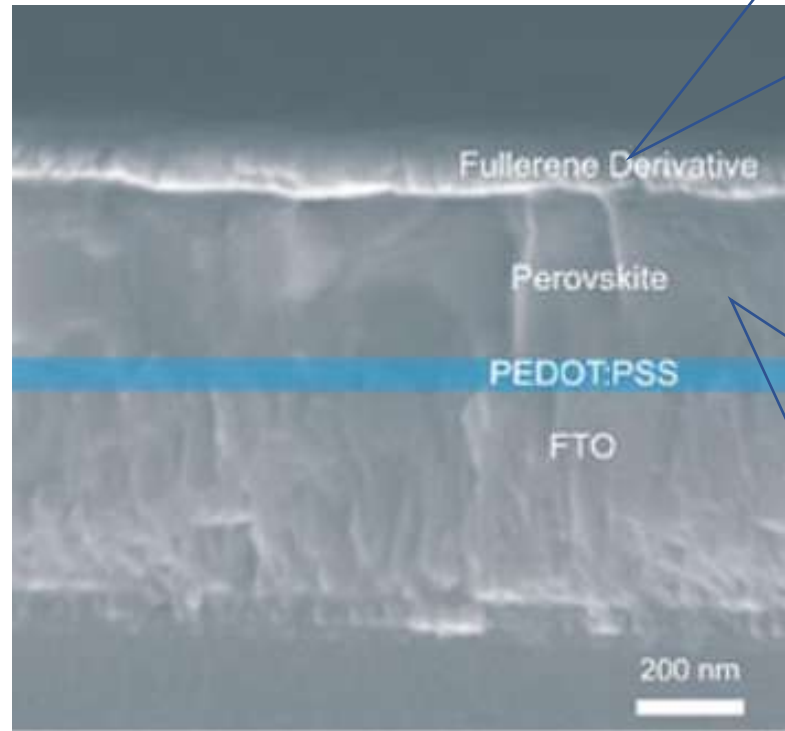
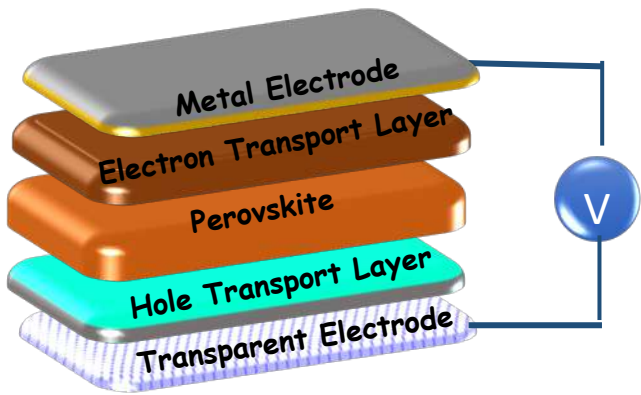


| Atoms | RMSD (Å) |
|-------|----------|
| Pb | 0.22 |
| I | 0.41 |

Thermal effect on the Electronic properties

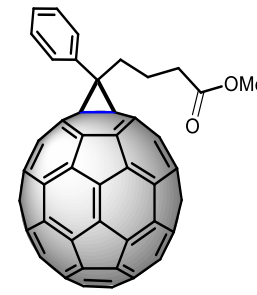


PEROVSKITE SOLAR CELLS



Cross-sectional SEM image of FTO/PEDOT-PSS/perovskite/fullerene derivatives

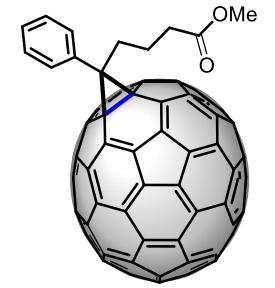
Tian, C. *et al.* ACS Appl. Mater. Interfaces 2016, 8, 31426-31432



PC₆₁BM

TiO_x/PC₆₁BM/Perovskite/Spiro/Au
PCE 17.9%

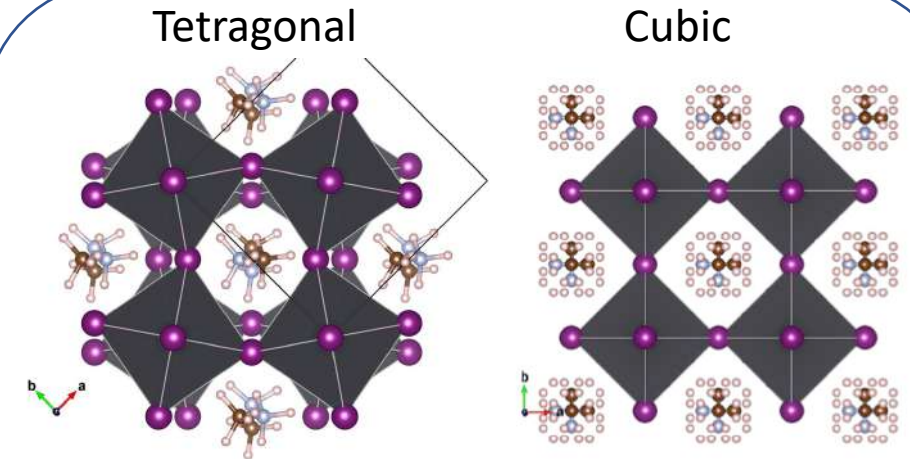
Sargent, E. H. *et al.* Energy Environ. Sci. **2015**, 8, 2365.



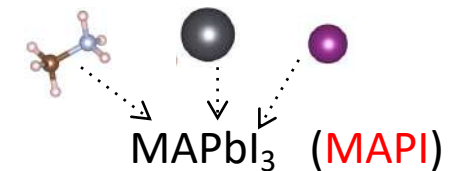
PC₇₁BM

PEDOT:PSS/Perovskite/PC₇₁BM/Ca/Al
PCE 16.3%

Wu, J. *et al.* J. Mater. Chem. A **2014**, 2, 15897.



Working conditions of the devices



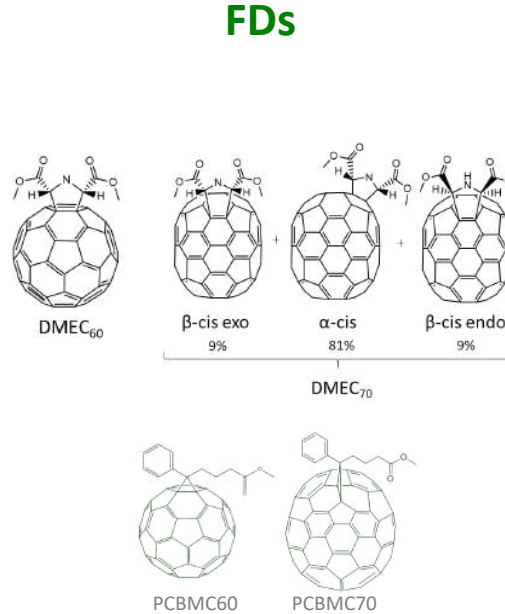
COMPUTATIONAL METHODOLOGY

Density Functional Theory (DFT)

- Plane waves basis set
- Pseudopotentials

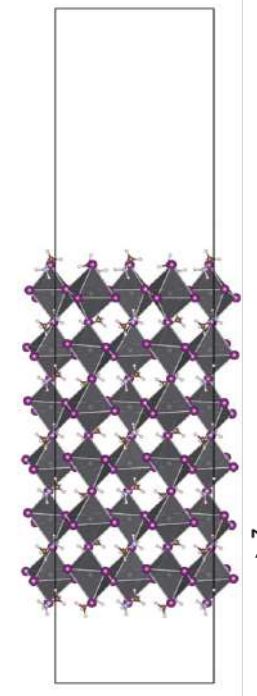
- ✓ Model structures: Isolated: HSE/6-31G(d) & PBC: optB88-vdW, $ecutwfn = 50$ Ry, $ecutrho = 400$ Ry, USPP
- ✓ Electronic properties: optB88-vdW; Hybrid: HSE06 / PBE0(α) + Spin-Orbit Coupling (SOC)

Computational packages: Gaussian 09, Quantum Espresso, VASP



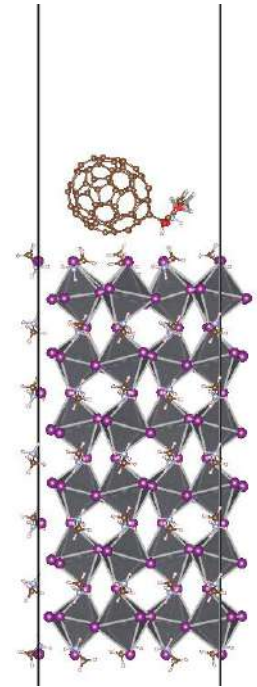
+

MAPI(001-MAI)
MAPI(001-Pbi)



→

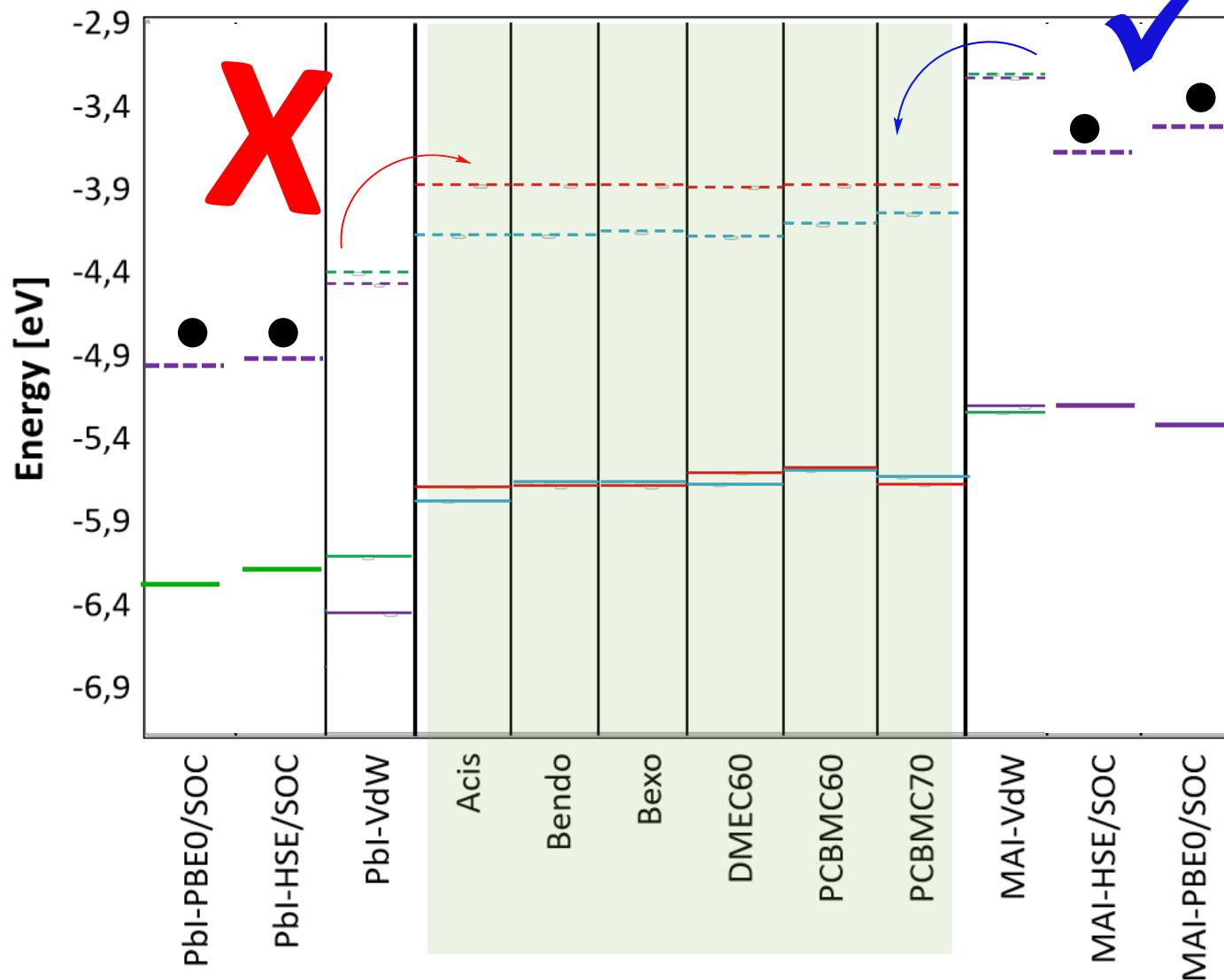
MAPI(001-MAI) / FDs
MAPI(001-Pbi) / FDs



BANDS ALIGNMENT

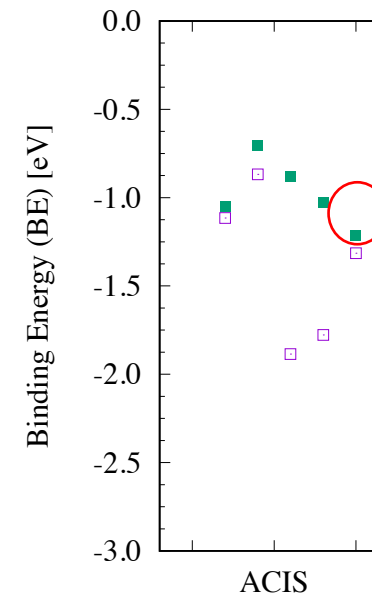
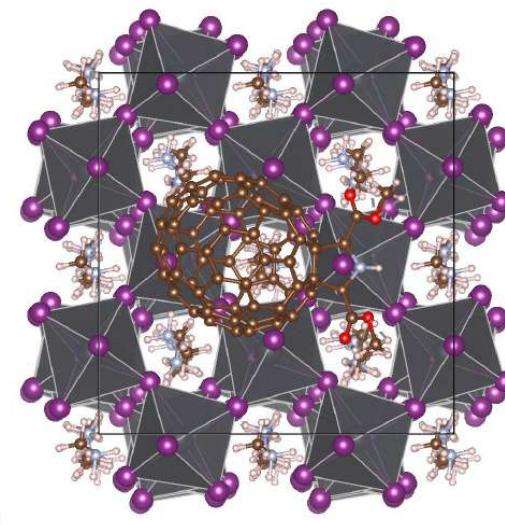
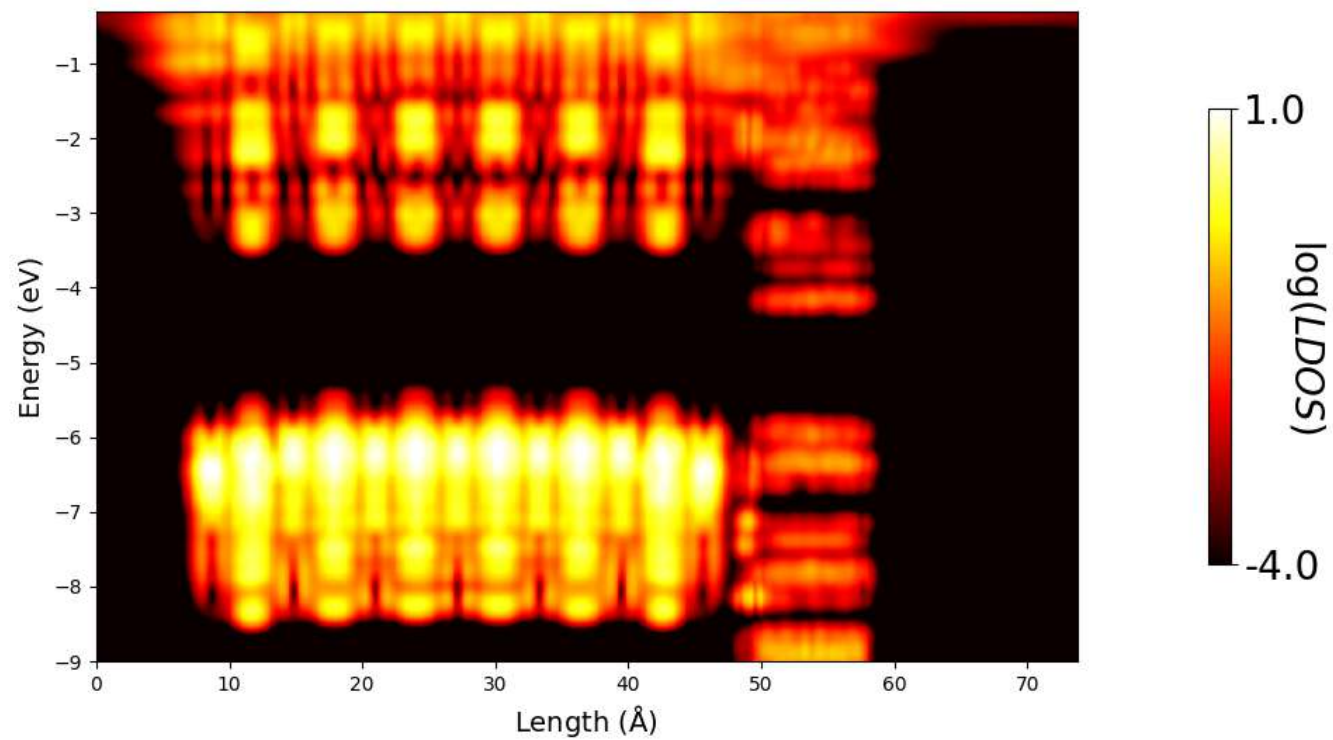
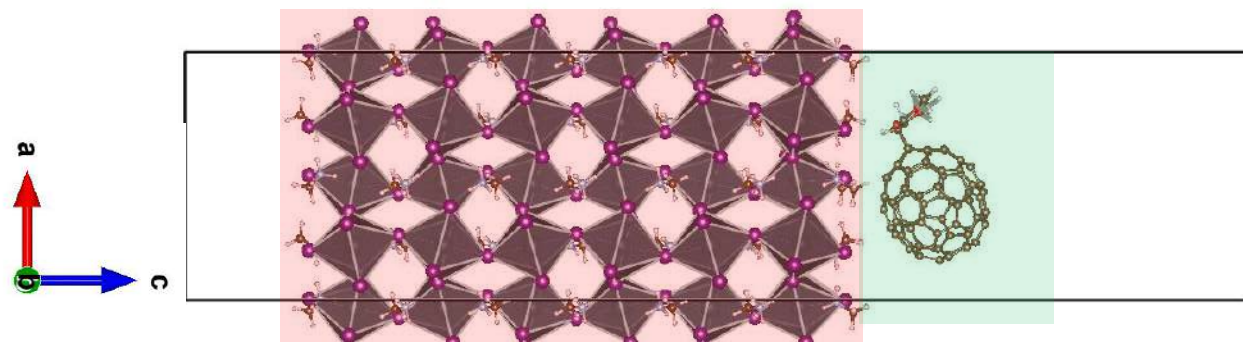
Bulk slab Theory Exp

Hybrid- SOC
corrections



- ✓ PBE0(α) - SOC , ENCUT=295 eV, PAW
- ✓ HSE06 – SOC, ENCUT=295 eV, PAW

Interface **MAPI(001-MAI)** / **ACIS** (Group down)



✓ optB88-vdW , ecutwfn = 50 Ry, ecutrho = 300 Ry, USPP

Acknowledgments

- CONICYT/FONDECYT Regular Grants No. 1130437, 1171807.
- CONICYT/FONDECYT Initiation Grant N.º. 11180984
- Nucleo Milenio Multimat
- Powered@NLHPC: This research was partially supported by the supercomputing infrastructure of the NLHPC (ECM-02).



Phys. Status Solidi B **252**, 2649-2656 (2015)

Phys. Status Solidi B **256**, 1800219 (2019)

Physica B **568**, 81 (2019)

Sci. Rep. **9**, 9194 (2019)